



# ALGEBRA I

## NYS REGENTS REVIEW

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Skill: Order of Operations

Use the order of operations to simplify the following expression.

$$32 - [(5 - 8)^2 + 2(3)]$$



Skill: Evaluating Expressions

Evaluate the expression for the given values.

$$\frac{a^2 - 4b}{2} \text{ if } a = 4 \text{ and } b = -$$



Regents Practice Questions

**Multiple Choice**

What operation should be done first in the expression  $2^3 - \frac{10}{2}$ ?

- (1) Adding  
(2) Subtracting  
(3) Dividing  
(4) Multiplying

**Constructed Response (2 pts)**

Michael was asked to solve the problem, evaluate  $3x^2 - 1$  when  $x = -2$ . Michael thinks the answer is  $-13$ . Is Michael correct? Explain your reasoning.

## Properties of Real Numbers

Number & Quantity: 2 – 8%



Skill: Identifying Properties

Fill in the blank with either the commutative, associative, or distributive property.

a.  $-2 + (x + y) = -2 + (y + x)$  \_\_\_\_\_ property of \_\_\_\_\_

b.  $2 \cdot (x \cdot y) = (2 \cdot x) \cdot y$  \_\_\_\_\_ property of \_\_\_\_\_

c.  $\frac{15x+30}{3} = 5x + 10$  \_\_\_\_\_ property of \_\_\_\_\_



Skill: Distributive Property

Simplify the expression using the distributive property. Combine like terms if needed.

$$-2(2x + 4) + 6(f -$$



Regents Practice Questions

### Multiple Choice (2pts)

When Ryan is solving the equation  $x^2 + 12x - 6 = 4x$ , he writes  $x^2 + 12x - 6 = 4x$ . Which property justifies Ryan's first step?

- (1) Commutative Property of Addition  
(2) Distributive Property of Addition  
(3) Associative Property of Addition  
(4) Identity Property of Addition

### Constructive Response (2 pts)

Lily is trying to solve the equation  $4(2x - 1) - 1 = 11$  for  $x$ . Her work is shown below. In which two lines did Lily make a mistake? Explain which property was used incorrectly.

Between which two lines did Lily make a mistake? Explain which property was used incorrectly.

**Line 1**  $4(2x - 1) - 1 = 11$

**Line 2**  $4(2x - 1) = 12$

**Line 3**  $8x - 1 = 12$

**Line 4**  $8x = 13$

**Line 5**  $x = \frac{13}{8}$



## Skill: Translating Words to Algebra

Translate each of the statements below into algebraic equations.

- Nine less than “ $x$ ” is equal to 10 \_\_\_\_\_
- The quotient of 36 and “ $a$ ” is 4 \_\_\_\_\_
- Twice the sum of  $f$  and 6 is 18 \_\_\_\_\_



## Skill: Translating Algebra to Words

**Directions:** Translate each of the equations below into algebraic words.

a.  $3(k + 3) = 9$       b.  $4k - 1 = 1$



## Regents Practice Questions

**Multiple Choice (2pts)**

Jenna deposits \$500 into her bank account and withdraws  $w$  dollars every week,  $w$ . Which of the following expressions represents the amount of money in her bank account after  $w$  weeks?

(1)  $500 \cdot 50w$       (3)  $500 - 50w$

(2)  $500 - 50w$

Consider the response to Question 1.

Rachel went to the deli for lunch for her and her friends. She bought slices of pizza, soda, and bags of chips. She bought three times as many bags of chips as sodas, and two fewer pizza slices than

If  $x$  represents the number of sodas they bought, write an algebraic expression that represents the number of lunch items they bought in total.

## Classifying Numbers (Rational vs. Irrational)

Number & Quantity: 2 – 8%



Skill: Rational & Irrational Numbers

Identify whether each of the following numbers is rational or irrational.

a.  $.8\overline{6}$

b. 2.7

c.  $2\pi$

d.  $\sqrt{169}$

e. 8.54172948 ...

f.  $\frac{\pi}{3}$

g.  $\sqrt{2}$

h.  $\frac{3}{4}$



Regents Practice Questions

### Multiple Choice (2pts)

1. Which expression results in an irrational number?

(1)  $\sqrt{100} - \sqrt{25}$

(2)  $\sqrt{36} \cdot \sqrt{1}$

(3)  $\sqrt{5}$

(4)  $\sqrt{2} + \sqrt{8}$

2. Given  $M = \sqrt{100} + \sqrt{10}$ ,  $T = \sqrt{3} + \sqrt{14}$ ,  $H = \sqrt{121}$

Which expression results in a rational number?

(3)  $T + H$

(4)  $H + M$

Extended Response (2pts)

A teacher wants to write the following set of numbers on the board:

$$a = \sqrt{15} \quad b = 3.1 \quad c = \sqrt{81}$$

Explain why  $a + b$  is irrational, but  $b + c$  is rational.



### Skill: Solving Linear Equations

What is the solution to the equation  $\frac{2}{3}(x + \frac{6}{5}) = 5$ ?



### Skill: Solving Linear Equations with Variables on Both Sides

Solve algebraically for  $x$ :

$$-\frac{3}{5}(x - \frac{3}{5}x) = -\frac{1}{2}$$



### Regents Practice Questions

#### Multiple Choice (2pts)

1. Which value of  $x$  makes the equation  $\frac{x-2}{3} + \frac{1}{2} = \frac{5}{6}$  true?  
(A)  $-\frac{1}{2}$       (B)  $-\frac{5}{2}$

(2) 0  
(3) 1  
(4) 2

2. The value of  $x$  that satisfies the equation  $\frac{2}{3} = \frac{x+9}{15}$  is  
(1) 1      (3) 19

(2) -1      (4) -19

#### Extended Response (2 pts)

Solve the equation below algebraically for the exact value of  $x$ .

$$6 - \frac{3}{4}(x + 7) = 6x$$



Skill: Solving Literal Equations

The formula for the perimeter of a rectangle is  $P = 2w + 2l$ . Write a formula that can be used to find the length,  $l$ , in terms of  $P$ , and  $w$ .



Skill: Solving Literal Equations with Square Roots

The volume of a right circular cone can be calculated using the formula  $V = \frac{1}{3}\pi r^2 h$ . Write a formula that can be used to find the positive value for the radius,  $r$ , in terms of  $V$  and  $h$ .



Regents Practice Questions

### Multiple Choice (2pts)

Three students were asked to solve the equation  $\frac{y+1}{2} = \frac{x+3}{4}$  for  $y$ . Their responses are shown below.

- (1)  $y = \frac{x+3}{2} - 1$   
i.  $y = \frac{x+3}{2} - 1$   
ii.  $y = \frac{x+3}{4} - 1$   
iii.  $y = \frac{x+3}{4} + 1$

Which response correctly solves the equation?

- i., ii., and iii.  
(2) i. and ii.  
(3) i. and iii.  
(4) ii. and iii.

### Constructed Response (2 pts)

The formula for converting degrees Fahrenheit,  $F$  to degrees Kelvin,  $K$  is:

$$K = \frac{5}{9}(459.67 + F)$$

Solve for  $F$  in terms of  $K$ .